

TNT Rules

Specification: remove $\forall x:$ and replace x with any term you like

from $\forall a:(a \cdot 0)=0$ make $(SSS0 \cdot 0)=0$ or $(a \cdot 0)=0$ or $((Sb+a) \cdot 0)=0$

Generalization: add $\forall x:$ to a string when x is a free variable in it

from $a=0$ make $\forall a:a=0$ (can't always do this inside a fantasy)

Interchange: $\forall x:\sim$ and $\sim\exists x:$ are interchangeable

from $\sim\exists a:(a+0)=Sa$ make $\forall a:\sim(a+0)=Sa$

Existence: replace any term in a string by x and add $\exists x:$

from $(S0+S0)=SS0$ make $\exists a:(S0+a)=SS0$ or $\exists b:b=SS0$

TNT Rules

Symmetry: if $r=s$ is a theorem, so is $s=r$

from $(S0+S0)=SS0$ make $SS0=(S0+S0)$

Transitivity: if $r=s$ and $s=t$ are theorems, so is $r=t$

from $S(0+0)=(0+S0)$ and $(0+S0)=S0$ make $S(0+0)=S0$

Add S: if $r=t$ is a theorem, so is $Sr=St$

from $S0=0$ make $SS0=S0$

Drop S: if $Sr=St$ is a theorem, so is $r=t$

from $S(0+0)=S0$ make $(0+0)=0$